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Cosmological bounds on active-sterile neutrino mixing after Planck data

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Based on PLB 2013, arXiv1303.5368

A. Mirizzi, G. Mangano, N. Saviano, E. Borriello, C. Giunti, G. Miele and O. Pisanti

Experimental anomalies & sterile ν interpretation

Some experimental data in tension with the standard 3 ν scenario + oscillations

(...and sometimes in tension among themselves....)

1. $\bar{\nu}_e$ appearance signals

Kopp et al., 2013

- excess of $\bar{\nu}_e$ originated by initial $\bar{\nu}_\mu$: **LSND/ MiniBooNE**

A. Aguilar et al., 2001

A. Aguilar et al., 2010

2. $\bar{\nu}_e$ and ν_e disappearance signals

- deficit in the ν_e fluxes from **nuclear reactors** (at short distance)

Mention et al. 2011

Acero, Giunti and Lavder, 2008

- reduced solar $\bar{\nu}_e$ event rate in **Gallium experiments**

Giunti and Lavder, 2011

Kopp, et al. 2011

All these anomalies, if interpreted as oscillation signals, point towards the **possible** existence of **1** (or more) **sterile neutrino** with $\Delta m^2 \sim O(\text{eV}^2)$ and $\theta_s \sim O(\theta_{13})$

Many analysis have been performed \rightarrow **3+1, 3+2** schemes

see Kopp's talk

Radiation Content in the Universe

At $T < m_e$, the radiation content of the Universe is

$$\varepsilon_R = \varepsilon_\gamma + \varepsilon_\nu + \varepsilon_x$$

The **non-e.m.** energy density is parameterized by the effective numbers of neutrino species N_{eff}

$$\varepsilon_\nu + \varepsilon_x = \frac{7}{8} \frac{\pi^2}{15} T_\nu^4 N_{\text{eff}} = \frac{7}{8} \frac{\pi^2}{15} T_\nu^4 (N_{\text{eff}}^{\text{SM}} + \Delta N)$$

$N_{\text{eff}}^{\text{SM}} = 3.046$ *due to non-instantaneous neutrino decoupling*

(+ oscillations)

At $T \sim m_e$, e^+e^- pairs annihilate heating photons.

Since $T_{\text{dec}}(\mathbf{v})$ is close to m_e , neutrinos share a small part of the entropy release

Mangano et al. 2005

ΔN = Extra Radiation: axions and axion-like particles, **sterile neutrinos** (totally or partially thermalized), neutrinos in very low-energy reheating scenarios, relativistic decay products of heavy particles...

Cosmological hints for extra radiation

Extra d.o.f. (i.e. sterile neutrinos) impact the cosmological observables :

✓ **BBN** (through the expansion rate H and the direct effect of ν_e and $\bar{\nu}_e$ on the n-p reactions)

BBN(standard) \rightarrow

$$N_{\text{eff}} \leq 4$$

(at 95% C.L.)

Mangano and Serpico, 2011

Hamman et al., 2011

Pettini and Cooke, 2012

with only a small significance preference for $N_{\text{eff}} > \text{stand.value}$

✓ **CMB & LSS** (sound horizon, matter-radiation equality, anisotropic stress, damping tail, small scale matter PS)

Slight preference for $N_{\text{eff}} > 3.046$

Komatsu et al., 2008,

Komatsu et al., 2010

G. Hinshaw, et al. 2013

J.L.Sievers et al. 2013

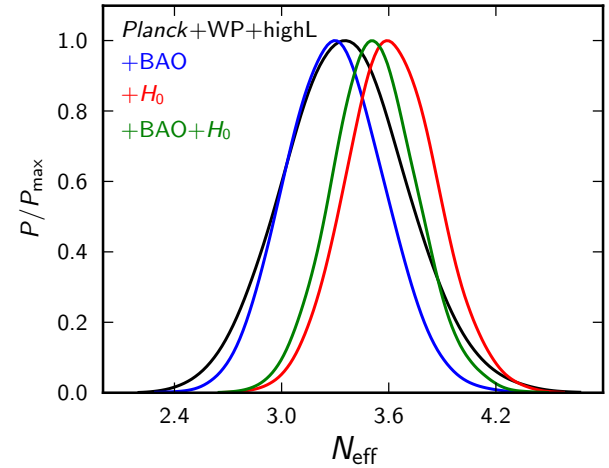
Hints for extra radiation reduce over the years

N_{eff} and Σm_ν constraints after Planck

$$N_{\text{eff}} = 3.30 \pm 0.54 \text{ (95 \% C.L.; Planck+WP+highL+BAO)}$$

→ compatible with the standard value at $1-\sigma$

Gorski & Lattanzi's talks



Planck XVI, 2013

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Including the H_0 value from HST...

$$N_{\text{eff}} = 3.52 \pm 0.48 \text{ (95 \% C.L.; Planck+WP+highL+BAO + } H_0 \text{)}$$

Indeed

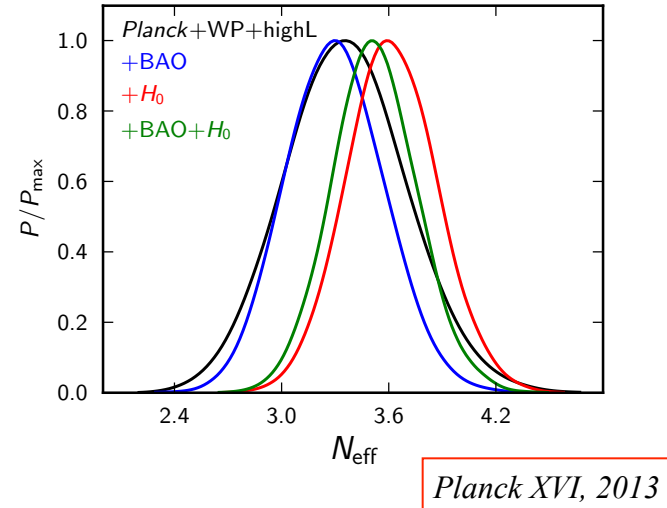
$$H_0^{\text{Planck}} = (63.3 \pm 1.2) \text{ km s}^{-1} \text{ Mpc}^{-1}$$

$$H_0^{\text{HST}} = (73.3 \pm 2.4) \text{ km s}^{-1} \text{ Mpc}^{-1}$$

Not trivial issue:

- unresolved astrophysical systematic effects
- beyond standard Λ CDM model (HOT DM: sterile)

see *M. Wyman et al., 2013* and *Hamann and Hasenkamp 2013*



N_{eff} and Σm_ν constraints after Planck

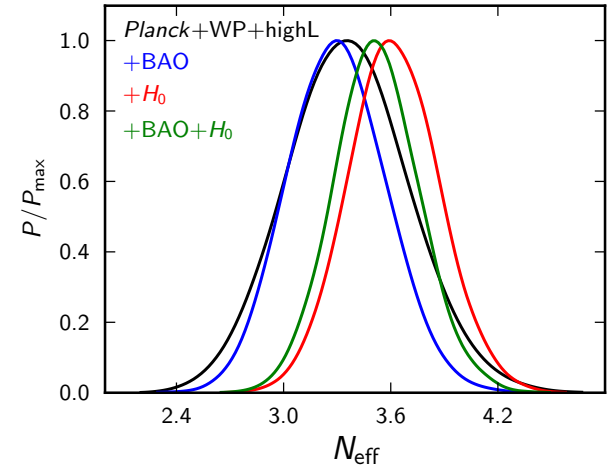
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Gorski & Lattanzi's talks

bounds on ν mass

model	Planck +	mass bound (eV) (95% C.L.)
3 degenerate ν_a	WP+HighL+BAO	$\Sigma m_\nu < 0.23$
Joint analysis N_{eff} & 3 degen ν_a	WP+HighL+BAO	$N_{\text{eff}} = 3.32 \pm 0.54$ $\Sigma m_\nu < 0.28$
Joint analysis N_{eff} & 1 mass ν_s	WP+HighL+BAO	$N_{\text{eff}} < 3.80$ $m_{\nu_s}^{\text{eff}} < 0.42$



Planck XVI, 2013

$$m_{\nu_s}^{\text{eff}} \equiv (94, 1 \Omega_\nu h^2) \text{eV}$$

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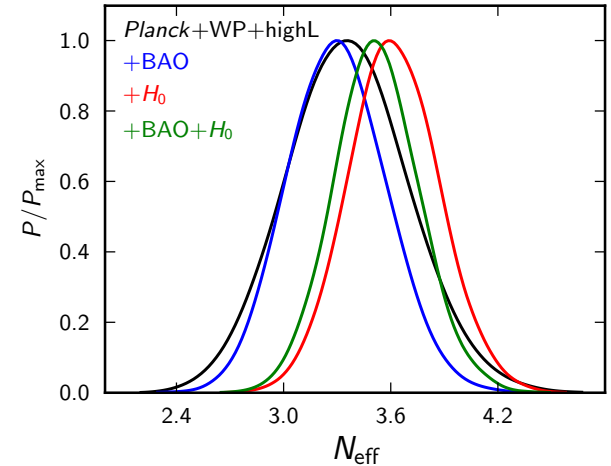
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Active-sterile flavor evolution

Sterile ν are produced in the Early Universe by the mixing with the active species

* No primordial sterile neutrino is present

- Describe the ν ensemble in terms of 4x4 density matrix $\varrho(x, y) = \begin{pmatrix} \varrho_{ee} & \varrho_{e\mu} & \varrho_{e\tau} & \varrho_{es} \\ \varrho_{\mu e} & \varrho_{\mu\mu} & \varrho_{\mu\tau} & \varrho_{\mu s} \\ \varrho_{\tau e} & \varrho_{\tau\mu} & \varrho_{\tau\tau} & \varrho_{\tau s} \\ \varrho_{se} & \varrho_{s\mu} & \varrho_{s\tau} & \varrho_{ss} \end{pmatrix}$
- introduce the dimensionless variables $x \equiv m a$; $y \equiv p a$; $z \equiv T_\gamma a$;
with $m =$ arbitrary mass scale; $a =$ scale factor, $a(t) \rightarrow 1/T$
- denote the time derivative $\partial_t \rightarrow \partial_t - H p \partial_p = H x \partial_x$, H the Hubble parameter $\boxed{\bar{H} \equiv \frac{x^2}{m} H}$

➤ the EoM become:

$$i \frac{d\varrho}{dx} = + \frac{x^2}{2m^2 y \bar{H}} [M^2, \varrho] + \frac{\sqrt{2} G_F m^2}{x^2 \bar{H}} \times \left[- \frac{8 y m^2}{3 x^2} \left(\frac{E_\ell}{m_W^2} - \frac{E_\nu}{m_Z^2} \right) + N_\nu, \varrho \right] + \frac{x \hat{C}[\varrho(y)]}{m \bar{H}}$$

Sigl and Raffelt 1993;

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with M neutrino mass matrix
 $U M^2 U^\dagger$

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MSW effect with background medium
(refractive effect)

charged lepton asymmetry subleading ($O(10^{-9})$) ➔

➔ 2th order term: “symmetric” matter effect

sum of e^- - e^+ energy densities ε

$$E_\ell \equiv \text{diag}(\varepsilon_e, 0, 0, 0)$$

Sigl and Raffelt 1993;

McKellar & Thomson, 1994

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refractive ν - ν term

self-interactions of ν with the ν background:
off-diagonal potentials \Rightarrow non-linear EoM

Sigl and Raffelt 1993;
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symmetric term

$$\propto (\varrho + \bar{\varrho})$$

Sigl and Raffelt 1993;

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asymmetric term

$$\propto (\varrho - \bar{\varrho}) \leftrightarrow L$$

Sigl and Raffelt 1993;

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Collisional term $\propto G_F^2$

creation, annihilation and all the momentum exchanging processes

Sigl and Raffelt 1993;
McKellar & Thomson, 1994
Dolgov et al., 2002.

Bounds on active-sterile mixing parameters after Planck

- ✓ sterile abundance by flavor evolution of the active-sterile system for 3+1 scenario (to be compared with the Planck constraints)
- ✓ 2 sterile mixing angles (+ 3 active) $10^{-5} \leq \sin^2 \theta_{i4} \leq 10^{-1}$ (i= 1,2)
- ✓ sterile mass-square difference $\Delta m_{\text{st}}^2 = \Delta m_{41}^2$ (+ 2 active) $10^{-5} \leq \Delta m_{41}^2 / \text{eV}^2 \leq 10^2$
- ✓ *average-momentum* approximation (single momentum): $\varrho_{\mathbf{p}}(T) = f_{FD}(p)\rho(T)$ ($\langle p \rangle = 3.15 T$)
- ✓ conservative scenario: vanishing primordial neutrino asymmetry

Mirizzi, Mangano, N.S. et al 2013, arXiv:1303.5368

Why is the multi-flavor system important ?

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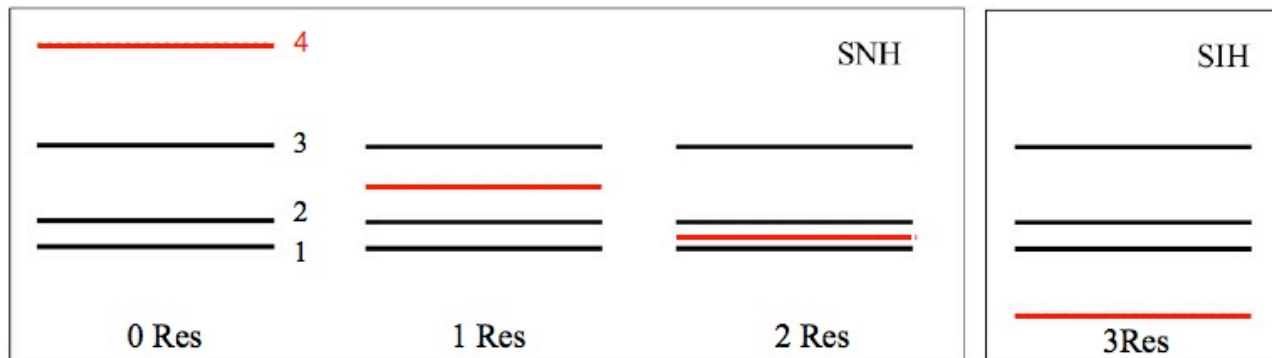
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NH

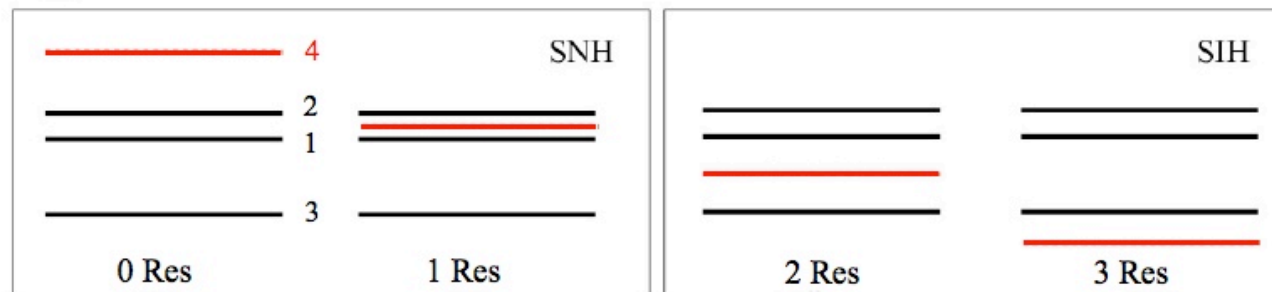


In the sterile sector:

resonances associated with

$$\Delta m_{4i}^2 \quad \theta_{i4} \quad i=1,2,3$$

IH



Why is the multi-flavor system important ?

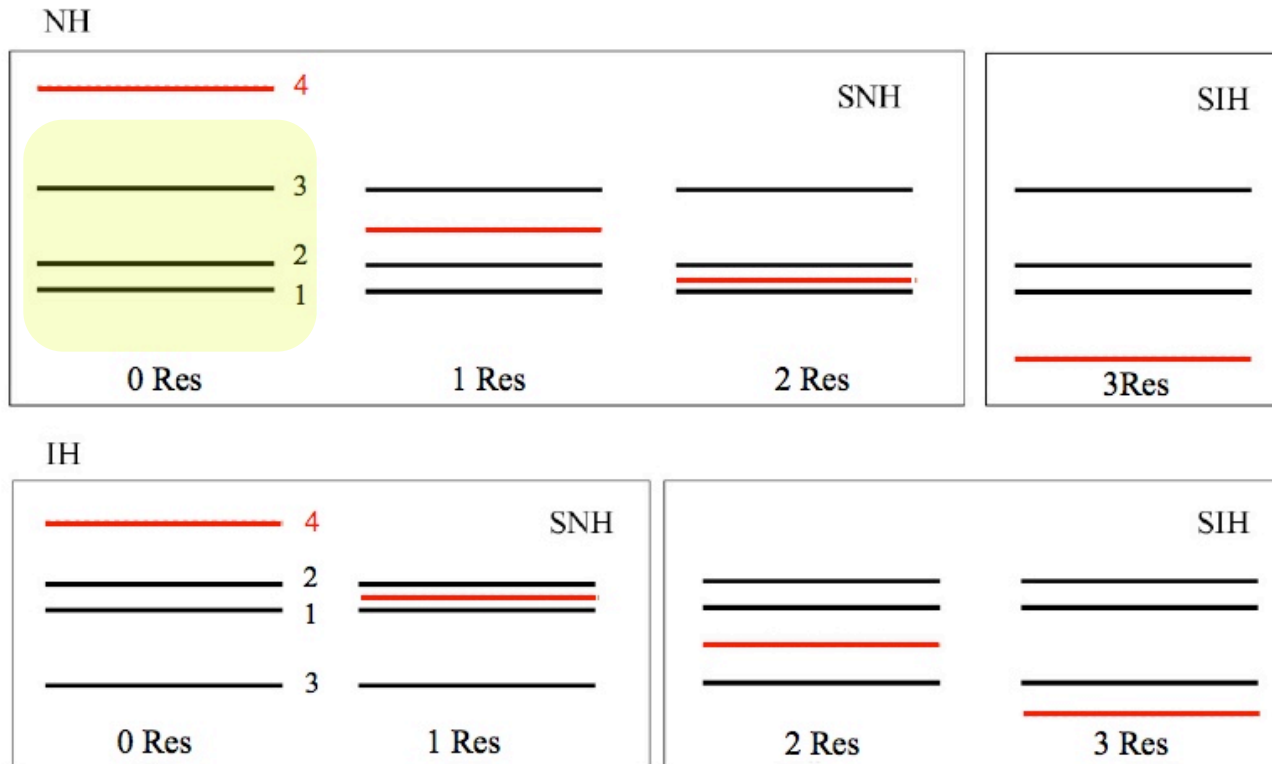
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In the sterile sector:

resonances associated with

$$\Delta m_{4i}^2 \quad \theta_{i4} \quad i=1,2,3$$

Active

NH, $\Delta m_{31}^2 > 0$
IH, $\Delta m_{31}^2 < 0$

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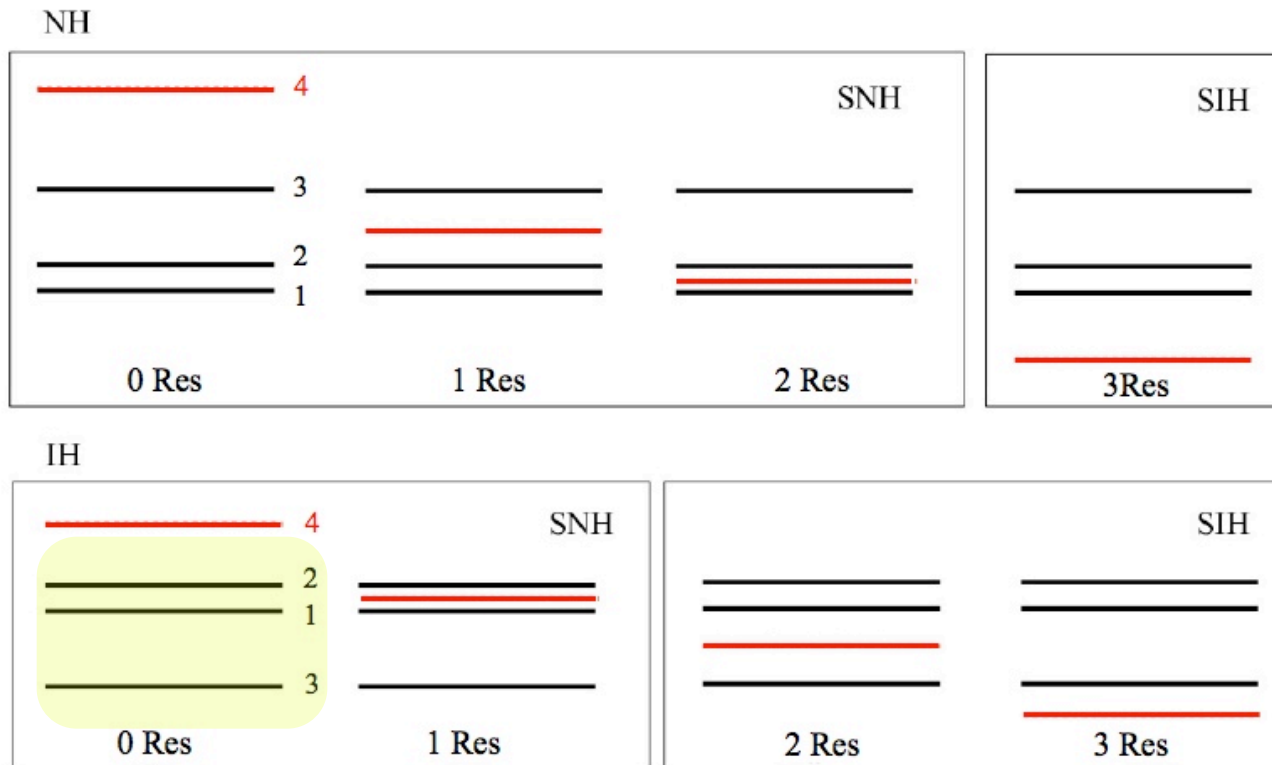
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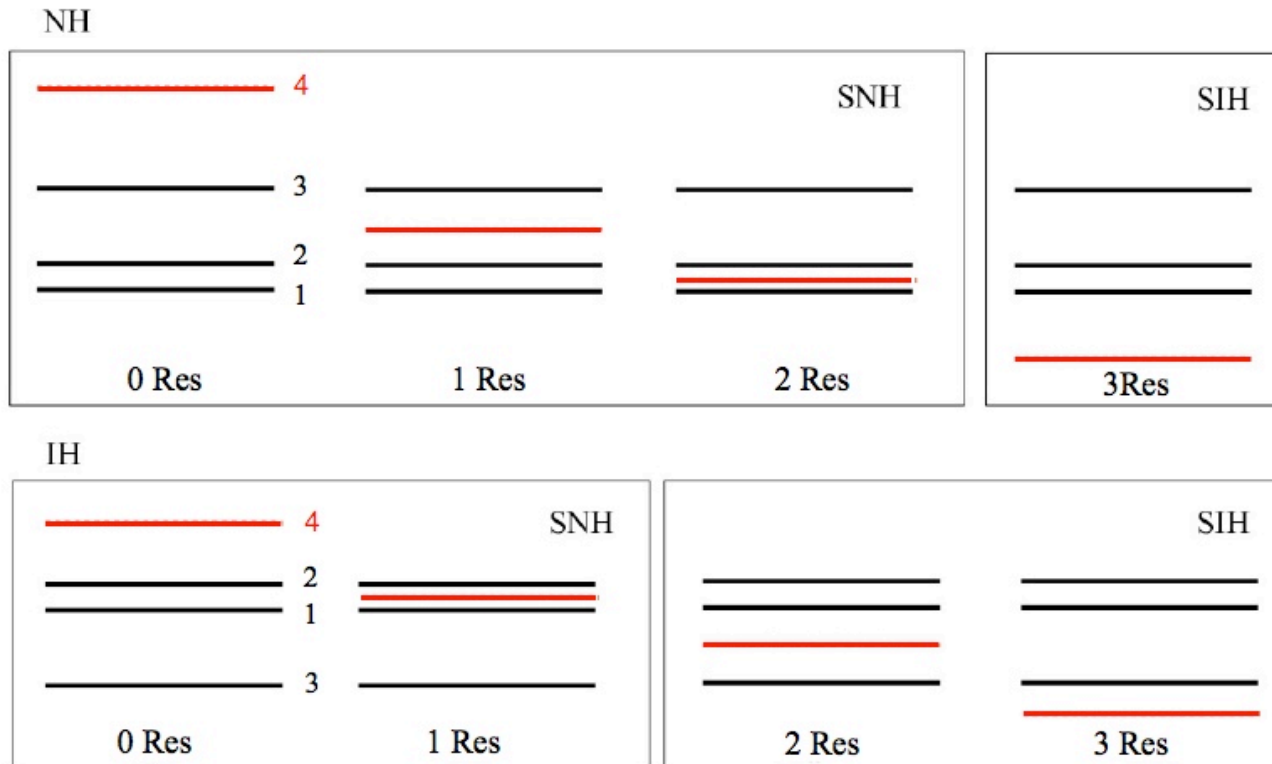
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In the sterile sector:

resonances associated with

$$\Delta m_{4i}^2 \quad \theta_{i4} \quad i=1,2,3$$

Active NH, $\Delta m_{31}^2 > 0$

Active IH, $\Delta m_{31}^2 < 0$

Sterile SNH, $\Delta m_{41}^2 > 0$

Sterile SIH, $\Delta m_{41}^2 < 0$

Sterile production: dependence on the active-sterile neutrino mass ordering

- The resonance condition can be satisfied only for $\Delta m^2_{4i} < 0$
- When more than one Δm^2_{4i} is negative, multiple resonances can occur

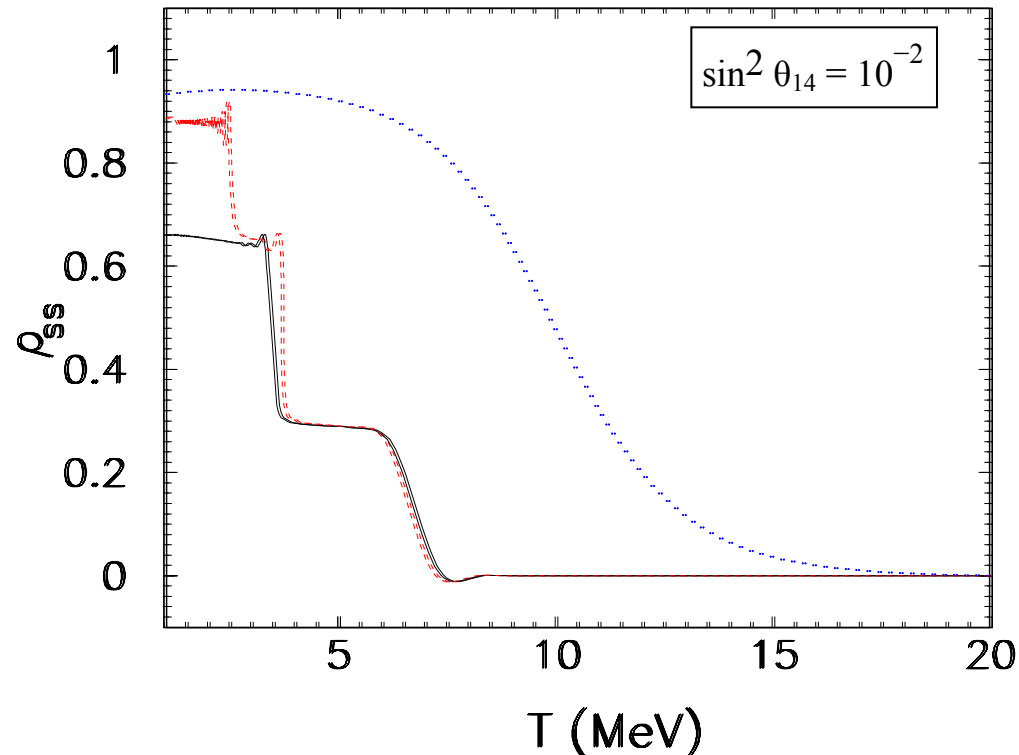
Evolution of sterile density component ρ_{ss} for 3 sterile mass splittings

$$\Delta m^2_{41} = 5 \times 10^{-2} \text{ eV}^2 \text{ (NO reson., NH + SNH)}$$

$$\Delta m^2_{41} = 10^{-5} \text{ eV}^2 \text{ (2 reson., NH + SNH)}$$

$$\Delta m^2_{41} = -10^{-5} \text{ eV}^2 \text{ (3 reson., NH + SIH)}$$

Mirizzi et al 2013, arXiv1303.5368

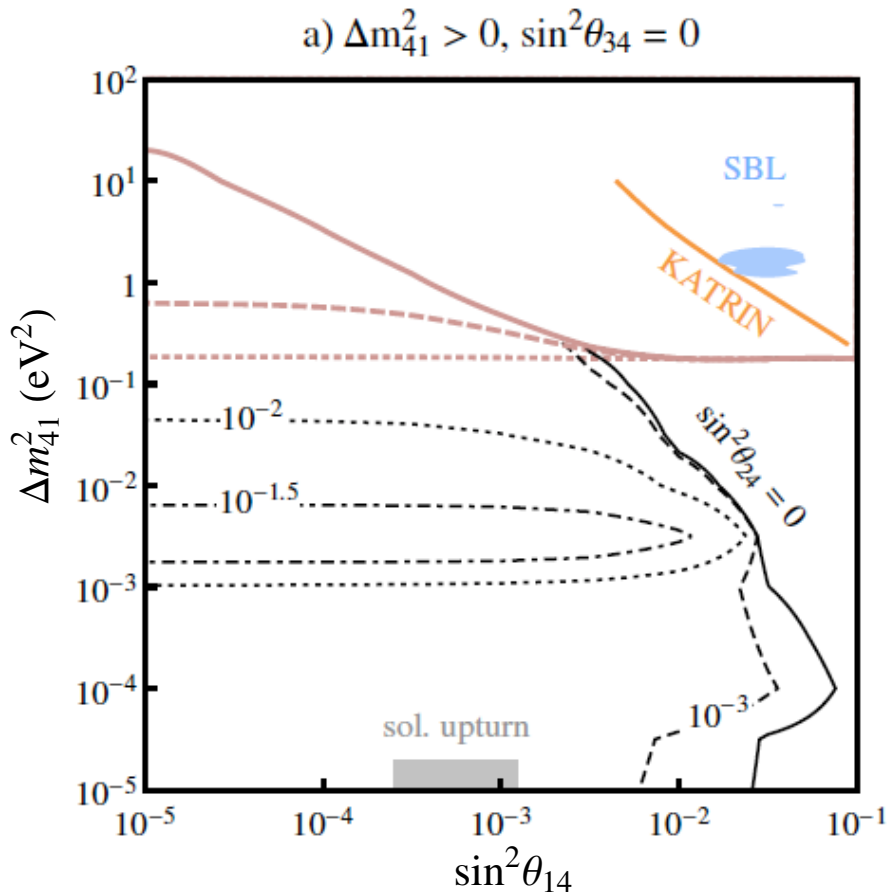


Bounds on active-sterile mixing parameters after Planck

... our results

Mirizzi et al 2013, arXiv1303.5368

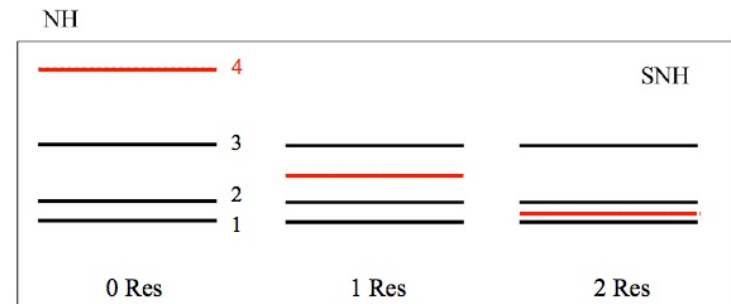
- ✓ Normal active hierarchy
- ✓ Normal sterile hierarchy



Radiation bounds

- Black curves imposing the 95% C.L. Planck constraint $N_{\text{eff}} < 3.8$ on ours $N_{\text{eff}} = \frac{1}{2} \text{Tr}[\rho + \bar{\rho}]$

The excluded regions are those on the right or at the exterior of the black contours.

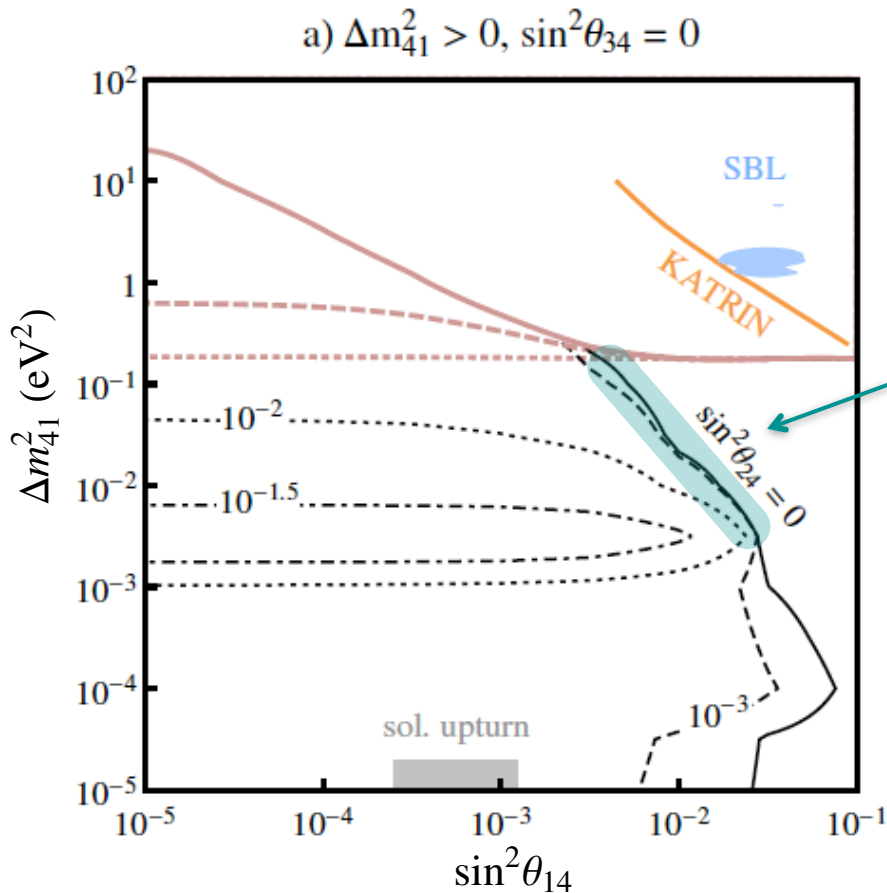


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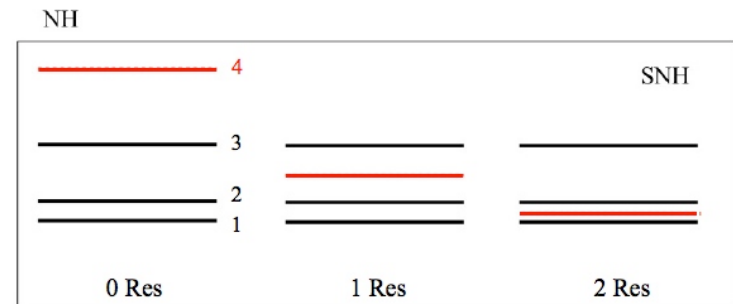
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- ✓ Normal active hierarchy
- ✓ Normal sterile hierarchy



simple behavior for
 $\theta_{24} \approx 0$ and for large sterile mass

see also Hannestad, Tamborra and Tram 2012



Radiation bounds

- Black curves imposing the 95% C.L. Planck constraint $N_{\text{eff}} < 3.8$ on ours $N_{\text{eff}} = \frac{1}{2} \text{Tr}[\rho + \bar{\rho}]$

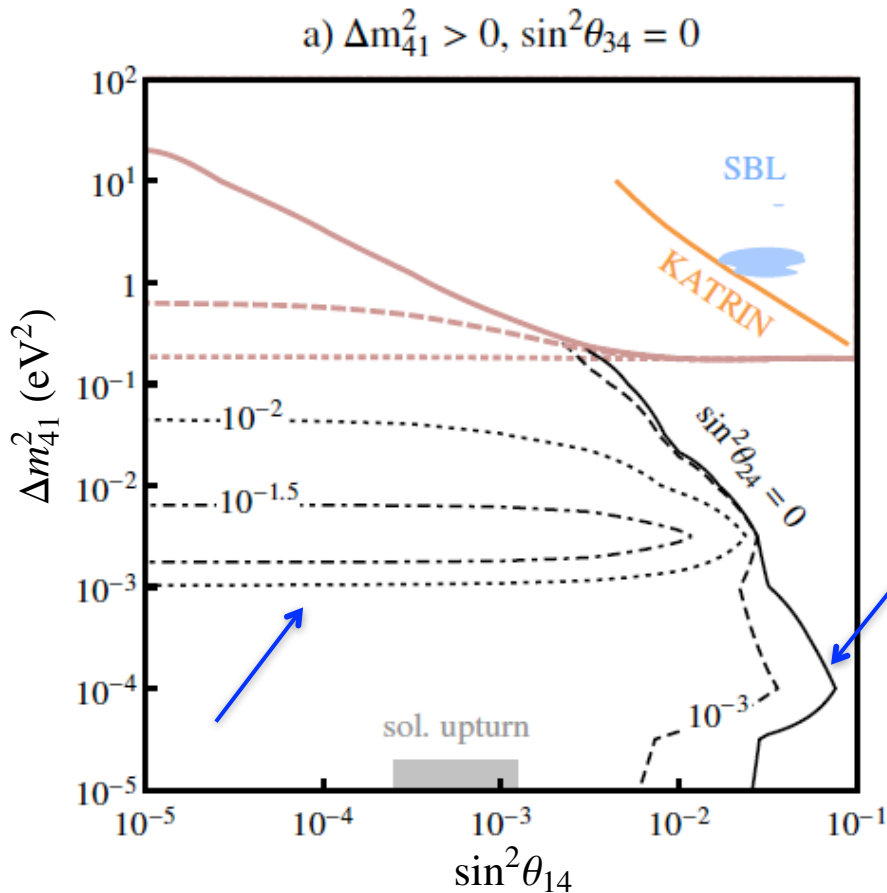
The excluded regions are those on the right or at the exterior of the black contours.

Bounds on active-sterile mixing parameters after Planck

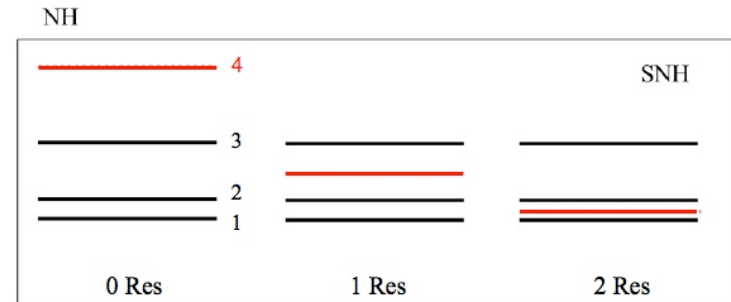
... our results

Mirizzi et al 2013, arXiv1303.5368

- ✓ Normal active hierarchy
- ✓ Normal sterile hierarchy



complex behavior for
small sterile mass due to resonances
and for $\theta_{24} > 0$



Radiation bounds

- Black curves imposing the 95% C.L. Planck constraint $N_{\text{eff}} < 3.8$ on ours $N_{\text{eff}} = \frac{1}{2} \text{Tr}[\rho + \bar{\rho}]$

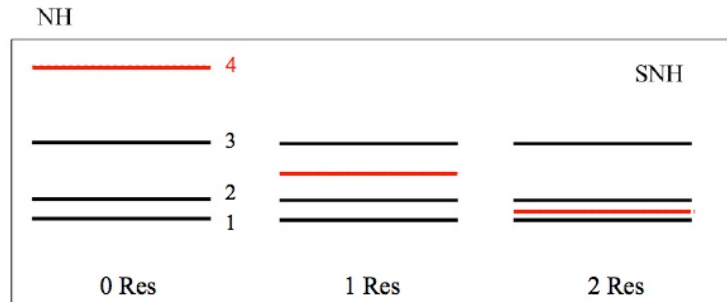
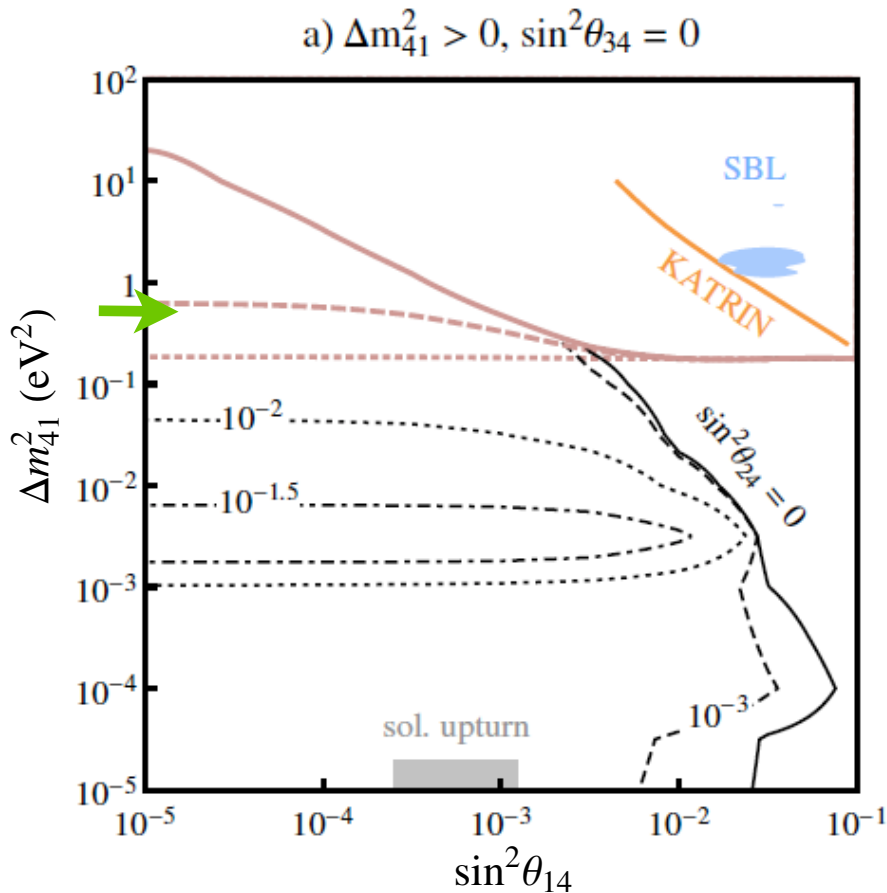
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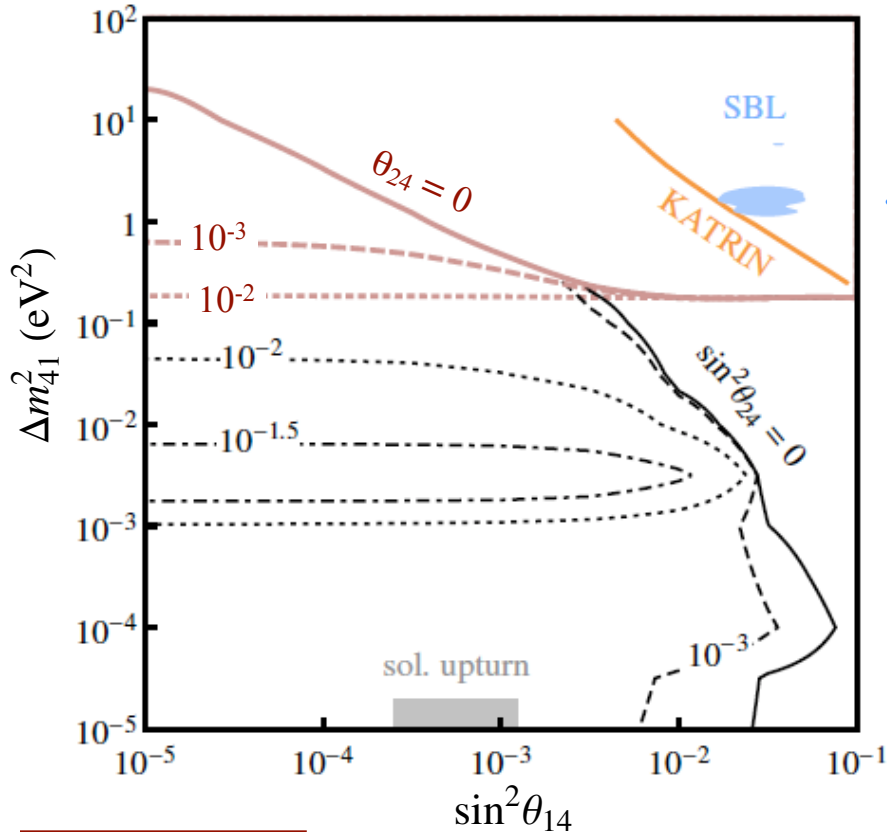
The excluded regions are those on the right or at the exterior of the black contours.

Note: above $m \sim \mathcal{O}(1 \text{ eV})$, sterile ν are not relativistic anymore at CMB \rightarrow **NO radiation constraint**

BUT mass constraints become important

Bounds on active-sterile mixing parameters after Planck

a) $\Delta m_{41}^2 > 0$, $\sin^2 \theta_{34} = 0$

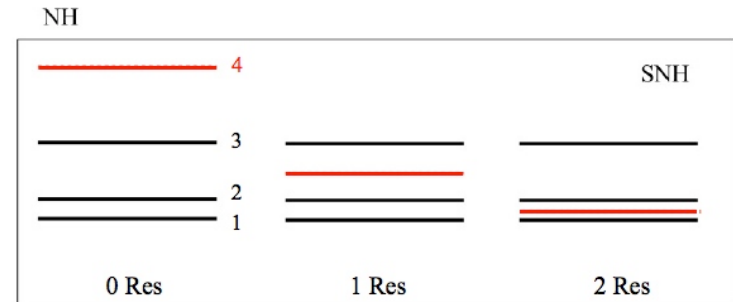


$\sin^2 \theta_{24} = 10^{-2}$, 95% C.L.
allowed region from
global analysis of SBL
(Giunti et al.)

... our results

Mirizzi et al 2013, arXiv1303.5368

- ✓ Normal active hierarchy
- ✓ Normal sterile hierarchy



Mass bounds

- Red curves imposing the 95% C.L. Planck constraint $m_{\nu s}^{\text{eff}} < 0.42 \Leftrightarrow \Omega_{\nu} h^2 < 4.5 \cdot 10^{-3}$ on ours

$$\Omega_{\nu} h^2 = \frac{1}{2} \frac{[\sqrt{\Delta m_{41}^2} (\rho_{ss} + \bar{\rho}_{ss})]}{94.1 \text{ eV}}$$

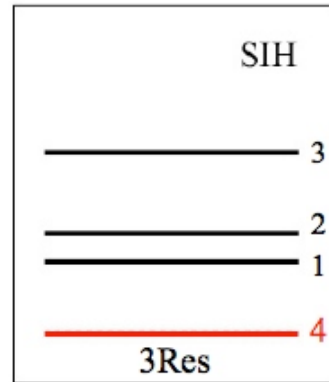
The excluded regions are those above the red contours.

Bounds on active-sterile mixing parameters after Planck

... our results

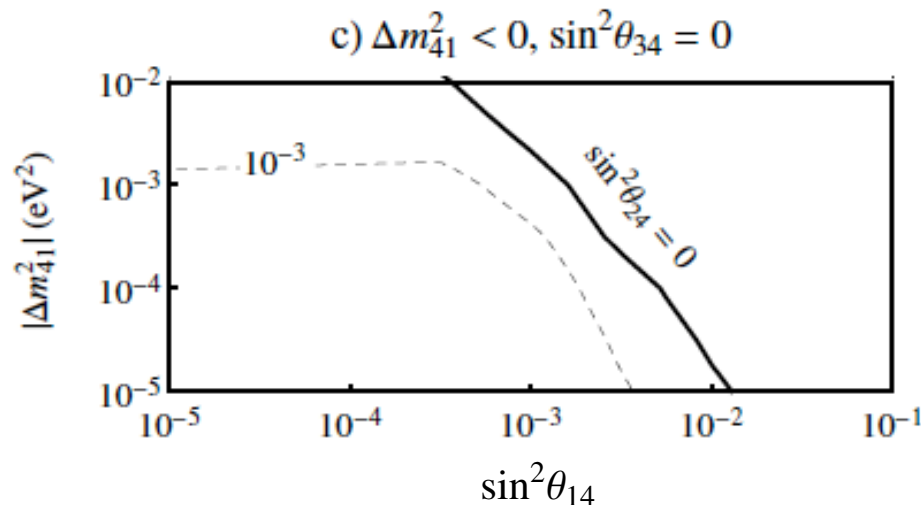
Mirizzi et al 2013, arXiv1303.5368

- ✓ Normal active hierarchy
- ✓ **Inverted** sterile hierarchy



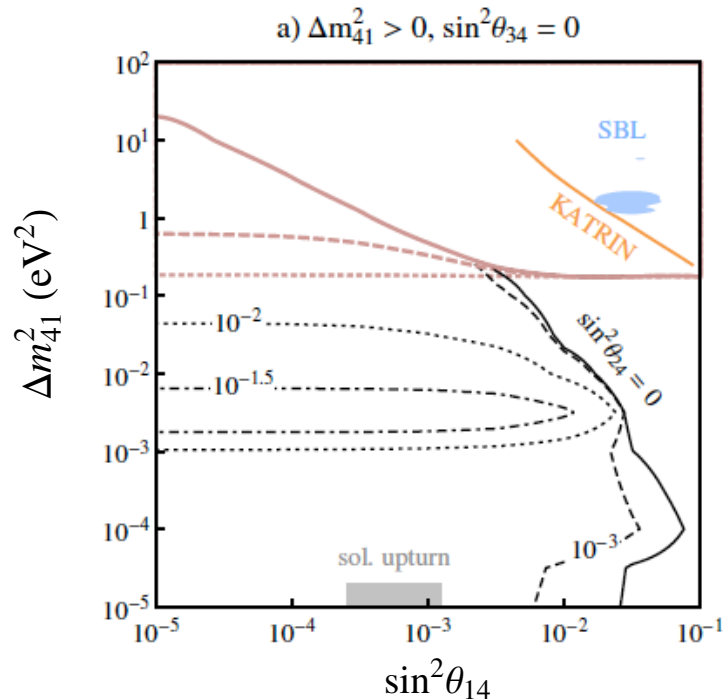
*additional 4-1 resonance:
increase of the sterile
production*

Radiation bounds



The excluded regions for the same values of the mixing angles are larger than the corresponding ones in the normal sterile hierarchy.

Bounds on active-sterile mixing: CONCLUSIONS



Mirizzi et al 2013,
arXiv:1303.5368

- *The sterile neutrino parameter space is severely constrained.*
- *Excluded area from the **mass bound** covers the region accessible by current and future laboratory experiments.*
- ***Sterile ν with $m \sim \mathcal{O}(1 \text{ eV})$ strongly disfavored***

Bounds on active-sterile mixing: the end of the story?

1. Suppression of the sterile production

✓ In the presence of large ν - $\bar{\nu}$ asymmetries ($\sim 10^{-2}$) sterile production strongly suppressed. Planck mass bound can be evaded *Mirizzi, N.S., Miele, Serpico 2012*

✗ Not trivial implication for BBN *Saviano et al., 2013*

2. If lab ν_s would be confirmed ...

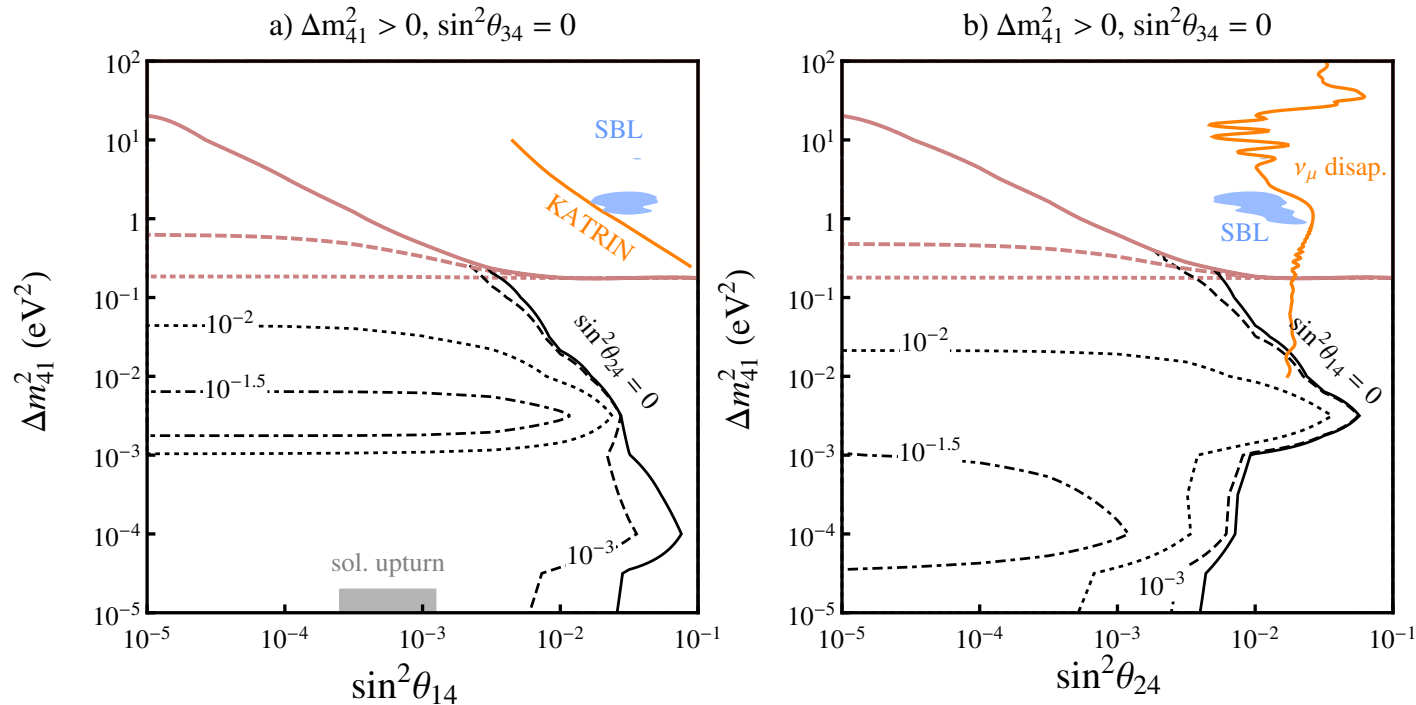
New physics in the particle sector and also modification of the standard cosmological model

The background is a soft, light blue gradient. It features several translucent, spherical bubbles of varying sizes, some of which are slightly out of focus. Thin, white, curved lines resembling light rays or motion paths sweep across the frame, adding a sense of dynamic movement. The overall aesthetic is clean, modern, and serene.

Thank you

Bounds on active-sterile mixing parameters after Planck

... our results



Mirizzi et al 2013,
arXiv:1303.5368

- Black curves imposing the 95% C.L. Planck constraint $N_{\text{eff}} < 3.8$ on ours $N_{\text{eff}} = \frac{1}{2} \text{Tr}[\rho + \bar{\rho}]$

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- Red curves imposing the 95% C.L. Planck constraint $m_{\nu_s}^{\text{eff}} < 0.42 \Leftrightarrow \Omega_\nu h^2 < 4.5 \cdot 10^{-3}$ on ours

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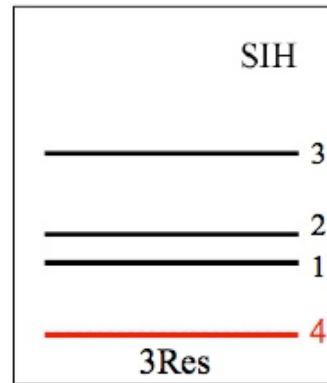
$$\Omega_\nu h^2 = \frac{1}{2} \frac{[\sqrt{\Delta m_{41}^2} (\rho_{ss} + \bar{\rho}_{ss})]}{94.1 \text{ eV}}$$

Bounds on active-sterile mixing parameters after Planck

... our results

Mirizzi et al 2013, arXiv1303.5368

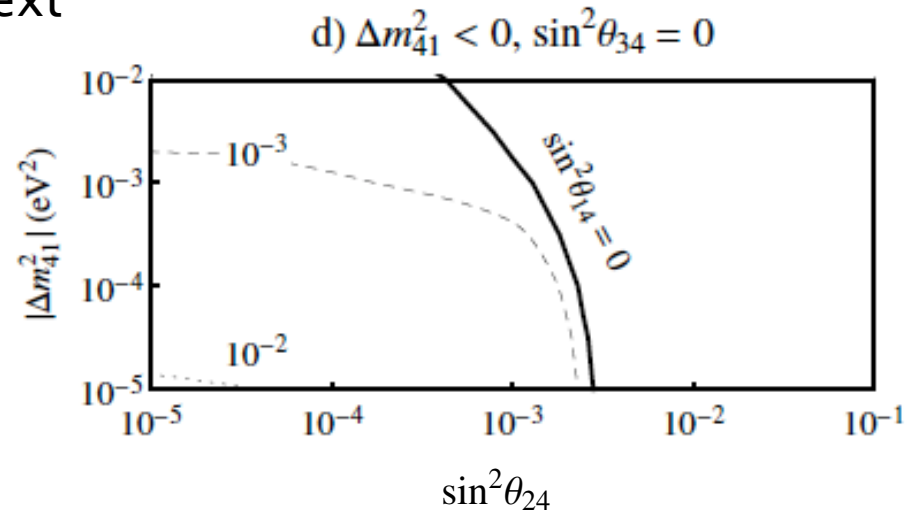
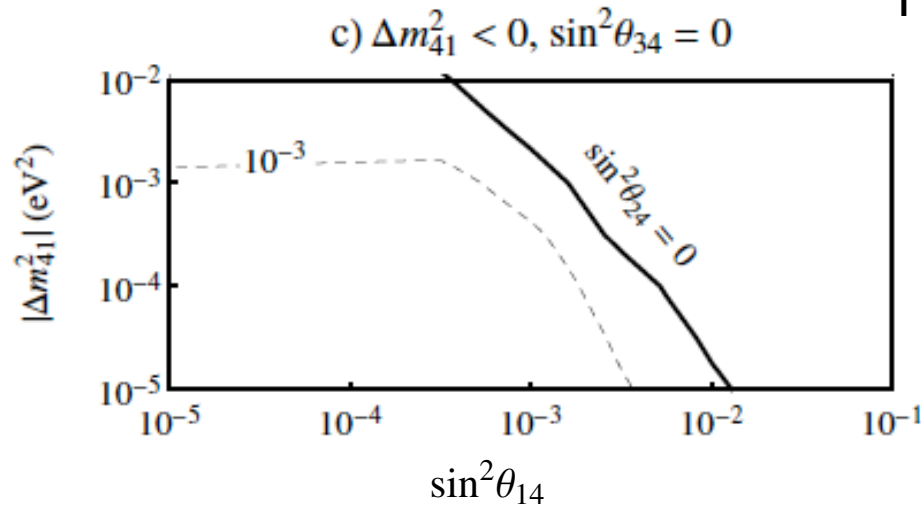
- ✓ Normal active hierarchy
- ✓ **Inverted** sterile hierarchy



*additional 4-1 resonance:
increase of the sterile
production*

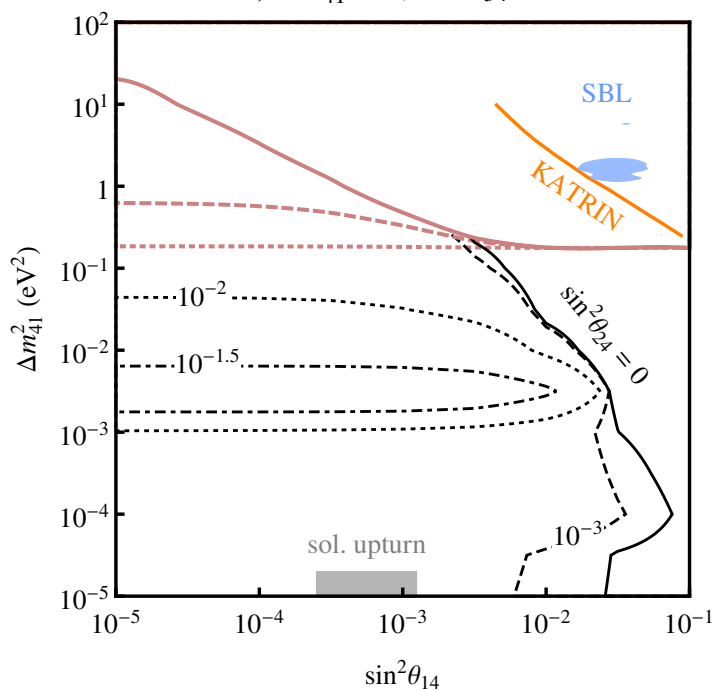
Radiation bounds

Text

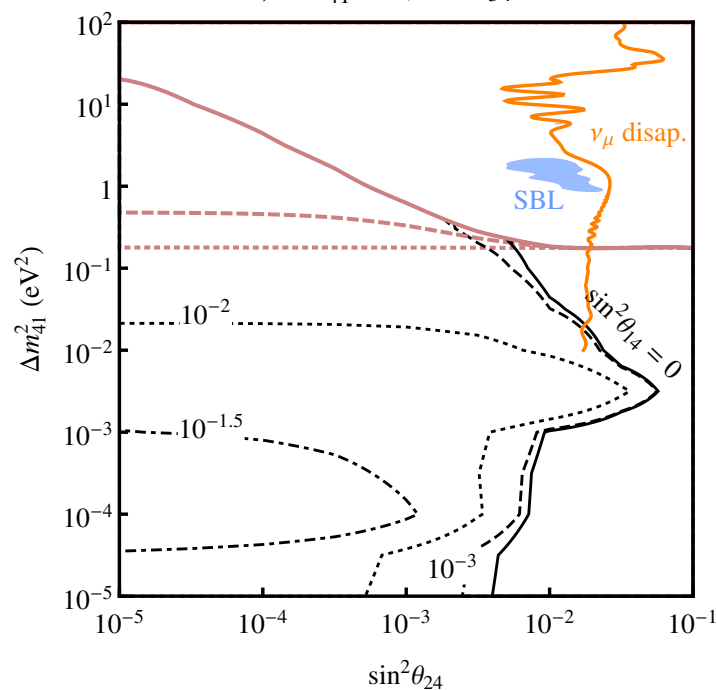


The excluded regions for the same values of the mixing angles are larger than the corresponding ones in the normal sterile hierarchy.

a) $\Delta m_{41}^2 > 0, \sin^2 \theta_{34} = 0$

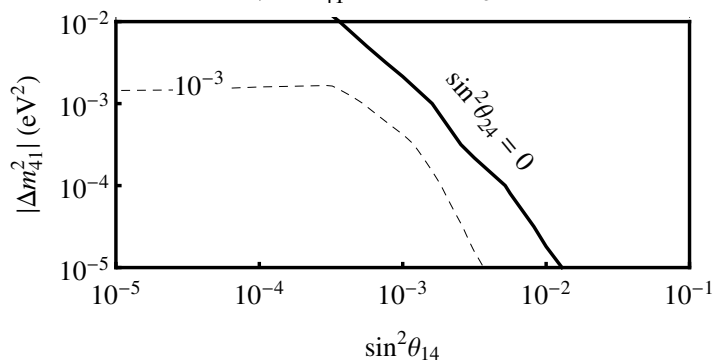


b) $\Delta m_{41}^2 > 0, \sin^2 \theta_{34} = 0$

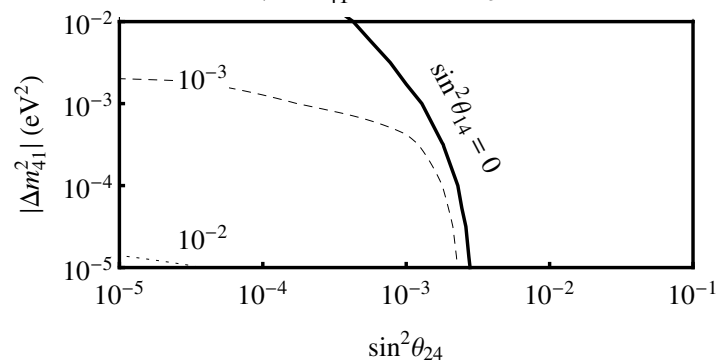


Sterile NH

c) $\Delta m_{41}^2 < 0, \sin^2 \theta_{34} = 0$



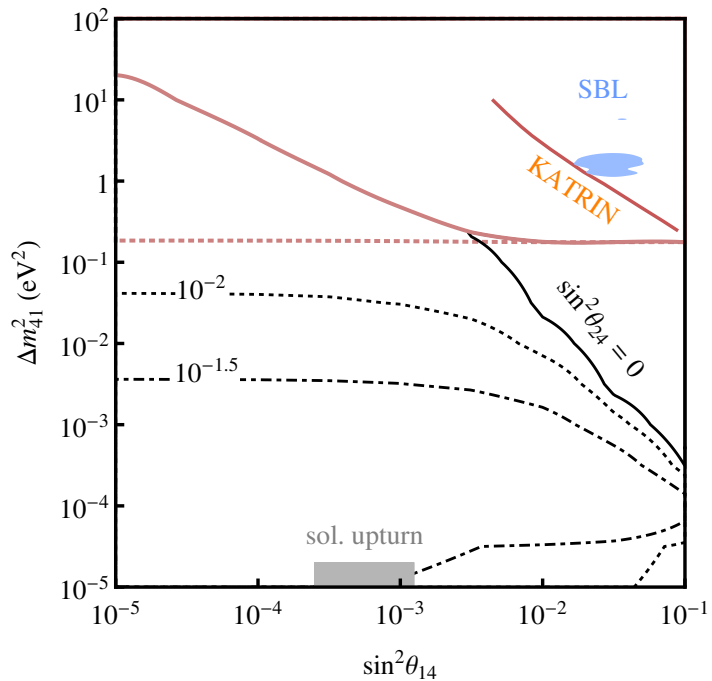
d) $\Delta m_{41}^2 < 0, \sin^2 \theta_{34} = 0$



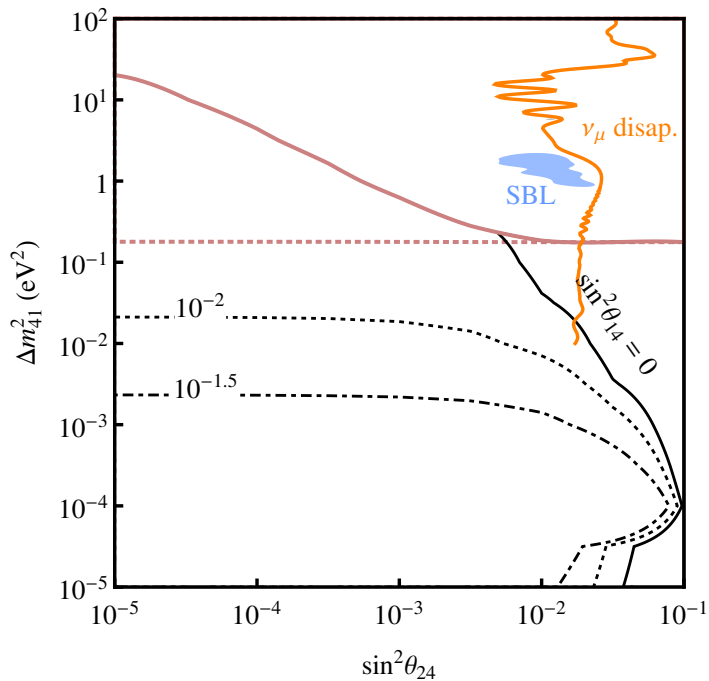
Sterile IH

Active IH

a) $\Delta m_{41}^2 > 0, \sin^2 \theta_{34} = 0$

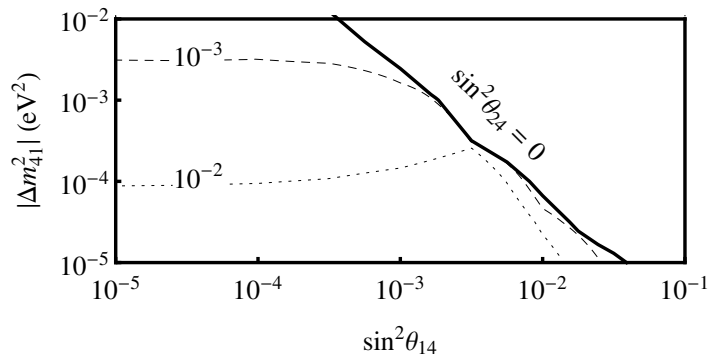


b) $\Delta m_{41}^2 > 0, \sin^2 \theta_{34} = 0$

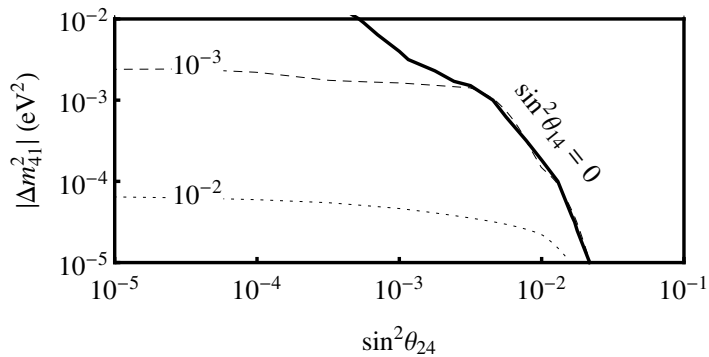


Sterile NH

c) $\Delta m_{41}^2 < 0, \sin^2 \theta_{34} = 0$

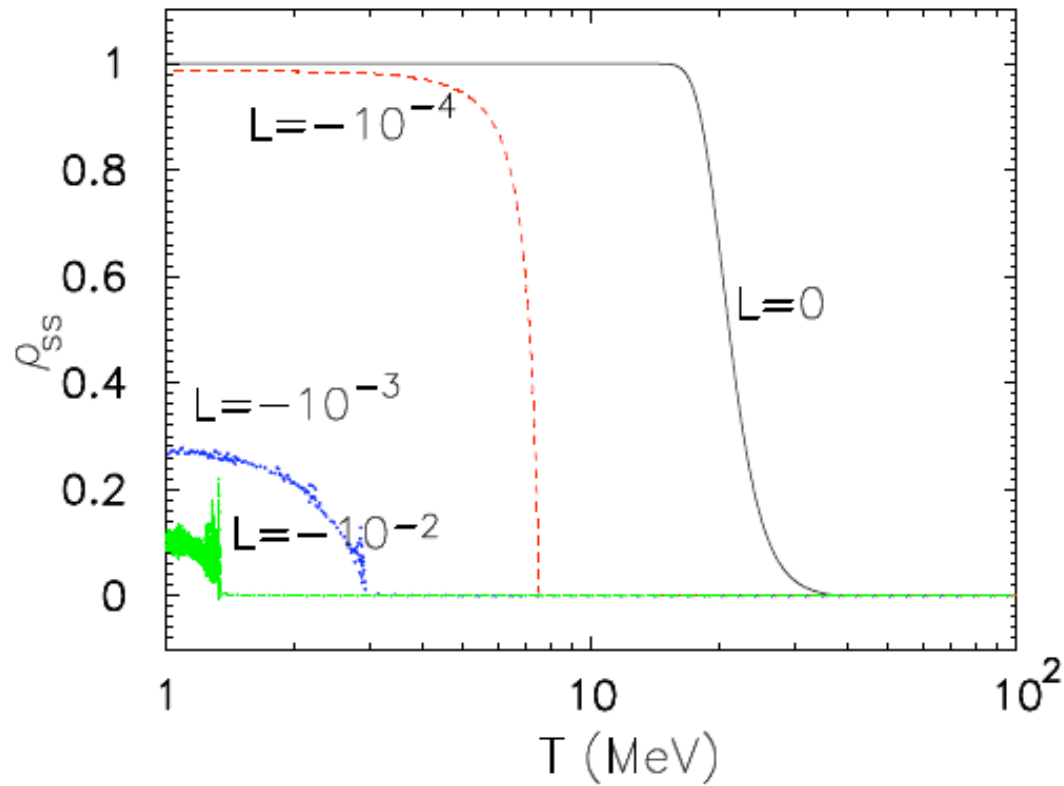


d) $\Delta m_{41}^2 < 0, \sin^2 \theta_{34} = 0$



Sterile IH

3 + 1 Scenario



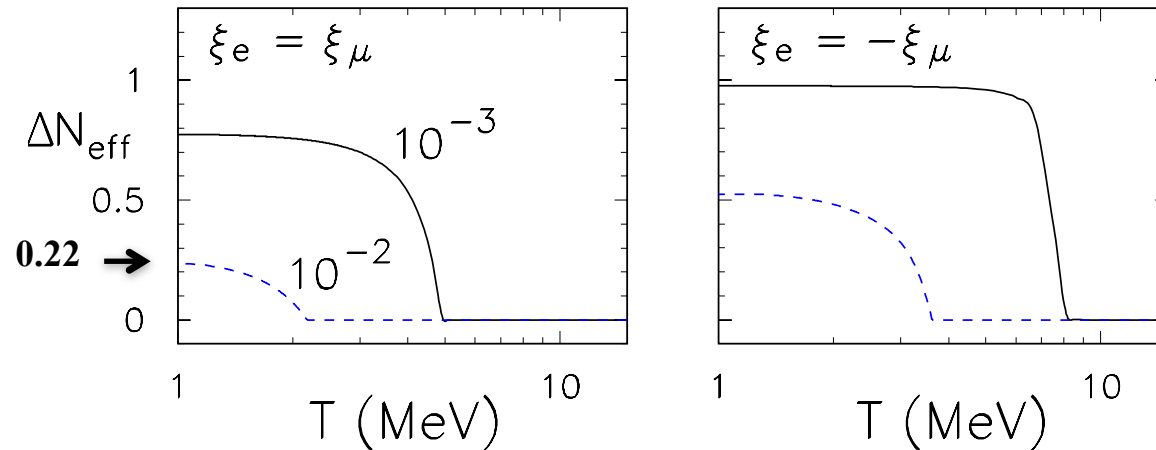
EXPLORATORY STUDY:
AVERAGE (or single)
MOMENTUM APPROX

Mirizzi, N.S., Miele, Serpico 2012
Phys. Rev. D 86, 053009

N_{eff} from multi-momentum treatment

- ✓ Compute N_{eff} as function of the ν *asymmetry parameter*

looking at the extra contribution $\Delta N_{\text{eff}} = \frac{60}{7\pi^4} \int dy y^3 \text{Tr}[\varrho(x, y) + \bar{\varrho}(x, y)] - 2$



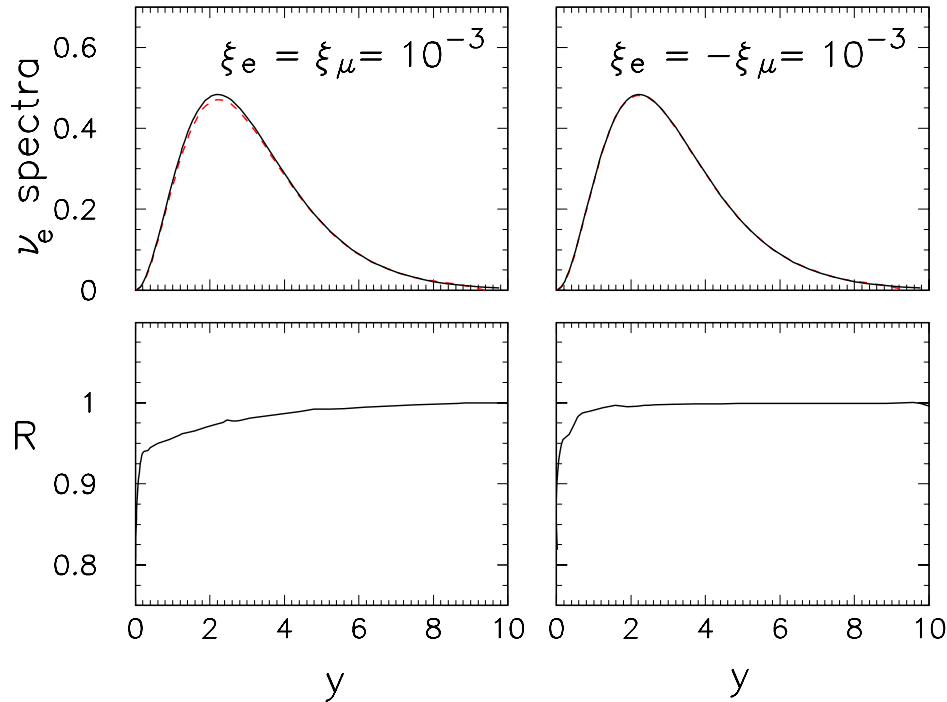
Case	ΔN_{eff}	$\Delta N_{\text{eff}}^{(y)}$
$ \xi \ll 10^{-3}$	1.0	1.0
$\xi_e = -\xi_\mu = 10^{-3}$	0.98	0.89
$\xi_e = \xi_\mu = 10^{-3}$	0.77	0.51
$\xi_e = -\xi_\mu = 10^{-2}$	0.52	0.44
$\xi_e = \xi_\mu = 10^{-2}$	0.22	0.04

Enhancement at most of 0.2 of unity for ΔN with respect to the single-momentum approx.

One needs to consider very large asymmetries in order to significantly suppress the production of sterile neutrinos.

see also Hannestad, Tamborra and Tram, 2012

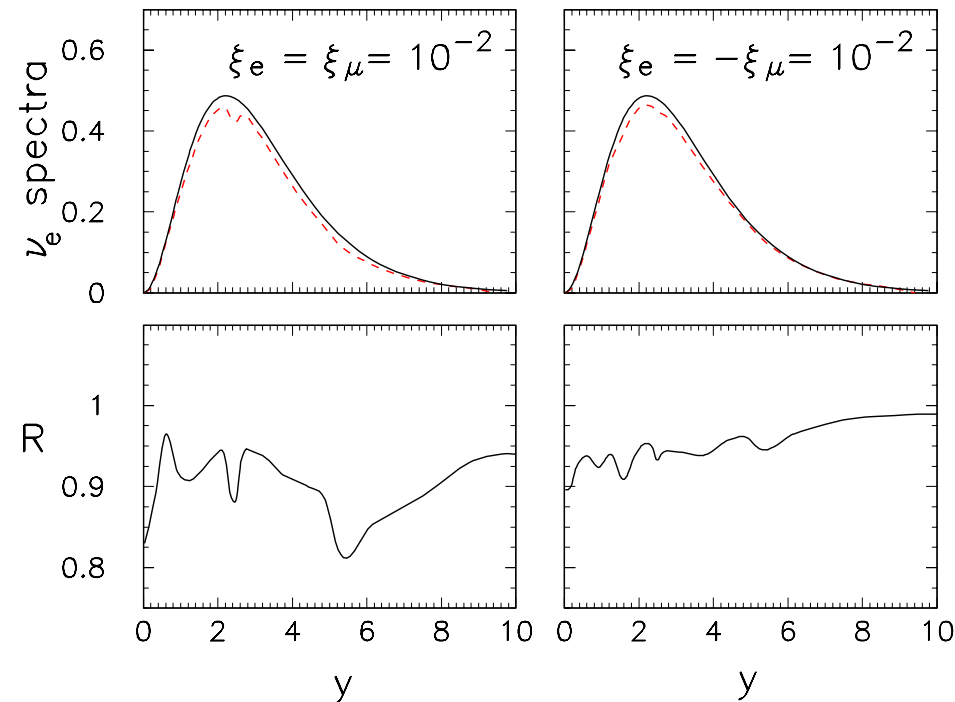
Spectral distortions



— $y^2 \rho_{ee}(y)$
 — $y^2 f_{eq}(y, \xi_e)$

$$\xi_v = \mu_v / T$$

$$R = \frac{\rho_{ee}(y)}{f_{eq}(y, \xi_e)}$$



Sizable distortions (especially for $\xi = 10^{-2}$)
 → consequences on primordial yields

Saviano et al, 2013; Phys. Rev. D 87, 073006

Non-trivial implications on BBN

Saviano et al, 2013;
Phys. Rev. D 87, 073006

Case	ΔN_{eff}	$\Delta N_{\text{eff}}^{(y)}$	Y_p	$^2\text{H}/\text{H} (\times 10^5)$
$ \xi \ll 10^{-3}$	1.0	1.0	0.259	2.90
$\xi_e = -\xi_\mu = 10^{-3}$	0.98	0.89	0.257	2.87
$\xi_e = \xi_\mu = 10^{-3}$	0.77	0.51	0.256	2.81
$\xi_e = -\xi_\mu = 10^{-2}$	0.52	0.44	0.255	2.74
$\xi_e = \xi_\mu = 10^{-2}$	0.22	0.04	0.251	2.64
$\xi_e = \xi_\mu = 10^{-3}, \text{ no } \nu_s$	~ 0	–	0.246	2.56
$\xi_e = \xi_\mu = 10^{-2}, \text{ no } \nu_s$	~ 0	–	0.244	2.55
standard BBN	0	0	0.247	2.56

PARthENoPE code *Pisanti et al, 2012*

$$Y_p = \frac{2(n/p)}{1+n/p}$$

Helium mass fraction

Deuterium mainly sensitive to the increase of N_{eff}

Helium 4 sensitive both to {

- increase of N_{eff}
- changes in the weak rates due to the spectral distortions